Fusing Learned Representations from Riesz Filters and Deep CNN for Lung Tissue Classification

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Abstract

A novel method to detect and classify several classes of diseased and healthy lung tissue in CT (Computed Tomography), based on the fusion of Riesz and deep learning features, is presented. First, discriminative parametric lung tissue texture signatures are learned from Riesz representations using a one-versus-one approach. The signatures are generated for four diseased tissue types and a healthy tissue class, all of which frequently appear in the publicly available Interstitial Lung Diseases (ILD) dataset used in this article. Because the Riesz wavelets are steerable, they can easily be made invariant to local image rotations, a property that is desirable when analyzing lung tissue micro-architectures in CT images. Second, features from deep Convolutional Neural Networks (CNN) are computed by fine-tuning the Inception V3 architecture using an augmented version of the same ILD dataset. Because CNN features are both deep and non-parametric, they can accurately model virtually any pattern that is useful for tissue discrimination, and they are the

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de facto standard for many medical imaging tasks. However, invariance to local image rotations is not explicitly implemented and can only be approximated with rotation-based data augmentation. This motivates the fusion of Riesz and deep CNN features, as the two techniques are very complementary. The two learned representations are combined in a joint softmax model for final classification, where early and late feature fusion schemes are compared. The experimental results show that a late fusion of the independent probabilities leads to significant improvements in classification performance when compared to each of the separate feature representations and also compared to an ensemble of deep learning approaches.

Keywords: texture signatures, classification, ILD, Deep Learning

1 1. Introduction

The White Book of the European Respiratory Society (ERS) mentions 2 respiratory diseases as one of the most common causes of premature mortal-3 ity. In 2008, one out every six deaths worldwide was attributable to them. 4 An annual cost of 380 billion Euros was associated with them in the Euro-5 pean Union alone, and this figure was estimated by taking into account the 6 loss of productive output, and the costs of direct medical care and $drugs^1$. 7 Battling these diseases is thus a priority in the healthcare domain. To combat 8 avoidable deaths and significant costs, obtaining an early accurate diagnosis 9 is essential. In such a scenario, clinicians may prescribe the correct treatment 10 as early as possible and thus limit disease progression. 11

¹European lung white book, http://www.erswhitebook.org/chapters/the-burden-of-lung-disease/, as of April 2018.

Respiratory ailments affecting the lung parenchyma are prevalent. One 12 of the largest and most diverse groups of such diseases is the set of Inter-13 stitial Lung Diseases (ILDs). They account for more than 200 pathologies 14 affecting the alveoli, the small lung airways, and the pulmonary intersti-15 tium (Kreuter et al., 2015). Information gathered from clinical, radiologi-16 cal, and pathological analyses are required to diagnose them accurately. In 17 particular, High-Resolution Computed Tomography (HRCT) images are the 18 radiological modality of choice for their characterization (Barr et al., 2016). 19 Some of the ailments may easily be misdiagnosed due to their rarity and 20 to the fact that radiologists are subjective when interpreting the content of 21 the images (Aziz et al., 2004; Watadani et al., 2013). Therefore, computer-22 ized assistance yielding exhaustive and reproducible image analysis has been 23 mentioned several times as beneficial for improving ILD management (De-24 peursinge et al., 2012c). 25

The task of classifying lung tissue pathologies benefits from recent ad-26 vances made in the area of visual pattern recognition. In the particular 27 context of texture and tissue characterization, the latter relies heavily on 28 the local organization of image directions at different scales (Blakemore and 29 Campbell, 1969; ter Haar Romeny, 2010), including local variations of pattern 30 properties such as local anisotropy (Depeursinge et al., 2014b; Depeursinge, 31 2017). Spatial domain representations of images alone provide insufficient in-32 formation to examine the local organization of scales and directions properly. 33 Therefore, to obtain a complete overview of the relationships between them, 34 intensity information needs to be complemented with information extracted 35 in the frequency domain.

Several authors exploit information embedded in the local organization 37 of scales and directions in images for pattern characterization and recogni-38 tion. Grey–Level Co–occurrence Matrices (GLCM) (Haralick et al., 1973), 39 Histograms Of Gradients (HOG) (Dalal and Triggs, 2005) used in the Scale-40 Invariant Feature Transform (SIFT) (Lowe, 2004), non-separable and sep-41 arable wavelets (Jeng-Shyang and Jing-Wein, 1999), Run–Length Encoding 42 (RLE) (Xu et al., 2004), and oriented filterbanks and wavelets (Gaussian, Ga-43 bor, Leung-Malik, Maximum Response (Cula and Dana, 2004; Leung and 44 Malik, 2001; Porter and Canagarajah, 1997; Randen and Husoy, 1999; Xu 45 et al., 2010) have been proposed for directional analysis. Unfortunately, sep-46 arable wavelets suffer from bias along the vertical and horizontal axes (Mal-47 lat, 1989), while the remainder requires an arbitrary choice of image direc-48 tions (Depeursinge et al., 2014b). Using a sequence of pixels along perimeters 49 of radius r, Local Binary Patterns (LBP) (Ojala et al., 2002) can perform 50 multi-directional analysis but they do not allow for multiresolution analysis, 51 easily. In addition, r is determined through costly optimization. Other meth-52 ods exploit the local organization of directions and scales indirectly. Notable 53 examples include Convolutional Neural Networks (CNN) (LeCun et al., 2004, 54 2010), Topographic Independent Component Analysis (TICA) (Hyvärinen 55 et al., 2001) and the scattering transform (Ablowitz et al., 1974; Ablowitz 56 and Segur, 1981). Despite their lack of interpretability, Deep Learning (DL) 57 models, and specifically CNNs, are now de facto standard methods for solv-58 ing challenging computer vision tasks due to the performance improvements 59 they bring when compared with most classic handcrafted feature approaches. 60 In recent years, these techniques have been successfully in many medical-61

domain tasks showing promising results and opening different research avenues (Greenspan et al., 2016; Litjens et al., 2017), particularly applied to
ILD as discussed later in the text below.

These results are now routinely encountered in the literature due to the 65 capacity of the deep architectures to learn a wide range of filters that respond 66 to complex patterns. Moreover, the increasing availability of medical datasets 67 allows this method to have more robust and precise results (Anthimopoulos 68 et al., 2016; Gao et al., 2016; Shin et al., 2016). For instance, CNNs have been 69 used for lung disease classification in (Gao et al., 2016), where performance 70 was not assessed explicitly and in (Li et al., 2014) with a reasonable degree 71 of success. Due to the flexibility of the features learned with deep learning 72 models having millions of parameters, they allow the representation of a large 73 number of patterns present in the dataset, which usually exacerbates the risk 74 of overfitting. 75

Another fundamental and general aspect that needs to be accounted 76 for is that the same texture pattern can appear at several local orienta-77 tions. Features that are locally rotation-invariant are desirable in such in-78 stances (Depeursinge et al., 2017b; Schmid, 2001). LBPs (Ojala et al., 2002) 79 and Rotation-covariant SIFT (RIFT) (Lazebnik et al., 2005) possess such 80 a property, but they do not model discriminative patterns specifically (i.e.,81 they yield handcrafted representations) and require exhaustive calculations. 82 Approaches based on steerable filters can achieve machine-precision, multi-83 directional and multi-scale characterization with invariance to local rota-84 tions (Depeursinge et al., 2017c; Do and Vetterli, 2002). 85

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Learned representations based on Riesz wavelets (Depeursinge et al.,

2014a), as used in this work, can precisely model multi-scale and multi-87 directional information that is important for tissue discrimination (Joyseeree 88 et al., 2018). Also, the obtained representation can easily be made invariant 89 to local rotations using the steerability of the models (see Section 2.2). One 90 drawback of Riesz representations is its reliance on parametric basis functions 91 with a potential lack of span. CNNs do not have invariance to local rotation 92 explicitly implemented. This can be alleviated up to a certain degree with ar-93 tificially augmented versions of the input with several rotations, but usually, 94 this is hard to do for small degrees of rotation. Additionally, CNN kernels 95 do not rely on parametric representations, and a large number of learned 96 filters can model virtually any pattern relevant to discrimination, under the 97 condition that the training dataset is large enough. The complementarity 98 of the two approaches motivates the fusion of the two representations into a 99 single model, which is also the main contribution of this article. 100

Five tissue types are often classified by the automatic methods found 101 in the literature using a publicly-available ILD dataset (Depeursinge et al., 102 2012c), as they have a more significant number of annotated regions than 103 other patterns: healthy, emphysema, ground glass, fibrosis, and micronod-104 ules. Some of the earliest of these papers (Depeursinge et al., 2007, 2008) 105 combined image data with clinical parameters to carry out classification. 106 This was followed by handcrafted steerable Riesz filterbanks (Depeursinge 107 et al., 2011a), low-level localized features (Depeursinge et al., 2011b) and 108 isotropic wavelet frames (Depeursinge et al., 2012b). After that, learned rep-109 resentations based on the Riesz transform (Depeursinge et al., 2012a) were 110 utilized. Recently, in (Joyseeree et al., 2018) a rotation-covariant approach 111

learning a class-wise texture signature using Riesz wavelets were proposed. 112 Here we build upon this work by complementing the features extracted us-113 ing a deep-learning network to extract high-level patterns not captured by 114 texture signatures. Other authors working on the same data include Song 115 et al. (Song et al., 2013) who first employed feature-based image patch ap-116 proximation. Li et al. (Li et al., 2013) then used automatic feature learning 117 followed by a customized CNN approach in (Li et al., 2014), while in (Song 118 et al., 2015), a locality-constrained subcluster representation ensemble is 119 used. Gao et al. use a deep CNN approach in (Gao et al., 2016). 120

The following publications use a different set of tissue types. A few clas-121 sify six tissue types by including the consolidation type. Examples of such 122 instances include Foncubierta et al. (Foncubierta-Rodríguez et al., 2012) who 123 used multi-scale visual words for classification and retrieval. Shin et al. (Shin 124 et al., 2016) used deep CNNs. Others used a significantly different set of 125 classes. For example, Anthimopoulous et al. (Anthimopoulos et al., 2016) 126 applied a deep CNN to the following classes: healthy, consolidation, honey-127 combing, micronodules, reticulation, ground glass, as well as a combination 128 of reticulation and ground glass. 129

To the best of our knowledge, there are not work in the literature exploiting the joint discriminative power of rotation invariant and deep learning representations for ILD classification. In summary, this paper describes a novel feature-fusion approach that exploits the complementarity of the learned representations from Riesz wavelets and fine-tuned deep CNNs to classify five tissue types associated with ILDs. We propose both early and late fusion strategies and estimate the performance with a four-fold crossvalidation setup. We compare all the methods using a softmax classifier
with the same hyperparameters to focus on the discriminatory power of the
extracted features.

The paper is organized as follows. In Section 2, we first present the 140 publicly available dataset used for the validation of our approach. This is 141 followed by an in-depth description of the theoretical aspects of the proposed 142 method. Section 3 presents the evaluation of classification performance, ob-143 served results, and statistical significance of the performance comparison. A 144 thorough analysis and interpretation of the observed behavior is carried out 145 in Section 4. Finally, conclusions are drawn based on the work done, and we 146 propose measures to improve performance in future work in Section 5. 147

¹⁴⁸ 2. Materials and Methods

149 2.1. Dataset and Validation Schemes

We use the most frequently used publicly-available ILD dataset (Depeursinge et al., 2012c) to evaluate the performance of the proposed methods. A slice of an HRCT series belonging to that dataset is shown in Fig. 1. It depicts the lung parenchyma of a patient that was annotated by an expert radiologist. The data set was used several times in past publications and these past approaches on the same data set will be briefly covered in this section.

To facilitate the comparison of our work with the majority of other techniques used on the ILD dataset, we carry out supervised learning on the following five expert-annotated classes: healthy, emphysema, ground glass, fibrosis, and micronodules. Moreover, these classes are most common in the ¹⁶¹ majority of the ILDs and are therefore relatively well represented regarding ¹⁶² the number of annotated regions available. An illustration of their respec-¹⁶³ tive appearances is provided in Fig. 2. One may observe that the visual ¹⁶⁴ differences between them are subtle, especially when comparing the healthy, ¹⁶⁵ emphysema, and micronodules classes.

For training and testing, four-fold cross-validation is employed. This en-166 tails extracting as many patches as possible from the annotated ILD images. 167 In the case of DL, a further augmentation step is taken whereby the patches 168 previously obtained are rotated by 90, 180, and 270 degrees. We also reflected 169 them along the vertical and horizontal axes. The new set of patches is then 170 divided into four groups according to two strategies. In the first one, they 171 are considered to be independent of each other, in line with what is often 172 encountered in the literature, and are divided into four equal sets. In the 173 second strategy, we ensure that the patches originating from an individual 174 patient only appear in one of the four groups to minimize the risk of inherent 175 bias. Two of the four groups are then concatenated and used for training the 176 classification model. One of the remaining sets is used for validation where 177 necessary, and the last one is used for testing the trained model. This process 178 is repeated four times to ensure that each group is once in the test set. 179

Finally, although the slice thickness and slice pixel dimensions of the HRCT protocol are all 1mm, the spacing between slices is 10mm. This implies that a considerable amount of information is missing between slices, which cannot be easily reconstructed. There is no possibility, therefore, to consider full 3D image analysis, which might lead to better results if the data are available.



Figure 1: Part of a slice taken from the ILD database that represents the right lung along with an expert annotation (red delineation) corresponding to a Region Of Interest (ROI) are presented here.



Figure 2: The five tissue classes selected for our work representing healthy parenchyma as well as emphysema, ground glass, fibrosis, and micronodules.

186 2.2. Tissue Characterization Using Riesz Filters

This section describes the approach to obtain learned discriminative and 187 locally rotation-invariant texture representations from Riesz wavelets and is 188 based on (Depeursinge et al., 2014a; Joyseeree et al., 2018). We first intro-189 duce the Riesz transform and its combination with radial wavelets to derive 190 steerable filterbanks in Section 2.2.1. Second, we describe in Section 2.2.2 191 how we learn one-versus-one class-specific discriminative texture signatures 192 from the parametric Riesz representation using Support Vector Machines 193 (SVM). 194

195 2.2.1. Steerable Riesz filterbanks

In a nutshell, Riesz filterbanks provide sets of image operators behaving like multi-scale local partial image derivatives of any order. Let $f(\boldsymbol{x})$ represent the function that models the content of a patch where \boldsymbol{x} represents pixel coordinates x_1 and x_2 . In other words, $f: \boldsymbol{x} \to f(\boldsymbol{x}), \boldsymbol{x} \in \mathbb{R}^2$, where $\boldsymbol{x} = (x_1, x_2)$.

Since the texture is encoded in the spatial transitions between the pixel values, the characterization of the imaging features may be achieved in the Fourier domain in terms of spatial frequencies. The Fourier domain representation of $f(\boldsymbol{x})$ is defined as

$$f(\boldsymbol{x}) \stackrel{\mathcal{F}}{\longleftrightarrow} \hat{f}(\boldsymbol{\omega}) = \int_{\mathbb{R}^2} f(\boldsymbol{x}) e^{-j\langle \boldsymbol{\omega}, \boldsymbol{x} \rangle} \, \mathrm{d}x_1 \mathrm{d}x_2, \tag{1}$$

where $\boldsymbol{\omega} = (\omega_1, \omega_2)$ and $\langle \cdot, \cdot \rangle$ denotes the dot product.

The Riesz filterbanks needed for our work are based on the real Riesz transform (Unser et al., 2011). The N + 1 components of the Nth-order ²⁰⁹ Riesz transform are based on the collection of operators $\mathcal{R}^{(n,N-n)}\{\cdot\}$ as

 $\boldsymbol{\mathcal{R}}^{N}\left\{f\right\}\left(\boldsymbol{x}\right) = \begin{pmatrix} \mathcal{R}^{(0,N)}\left\{f\right\}\left(\boldsymbol{x}\right) \\ \vdots \\ \mathcal{R}^{(n,N-n)}\left\{f\right\}\left(\boldsymbol{x}\right) \\ \vdots \\ \mathcal{R}^{(N,0)}\left\{f\right\}\left(\boldsymbol{x}\right) \end{pmatrix}, \qquad (2)$

with n = 0, 1, ..., N. A kernel $\mathcal{R}^{(n,N-n)} \{f\}(\boldsymbol{x})$ that represents the effect of a member of the filterbank on the input signal is defined in the spatial and Fourier domains as:

$$\mathcal{R}^{(n,N-n)}\left\{f\right\}(\boldsymbol{x}) \stackrel{\mathcal{F}}{\longleftrightarrow} \mathcal{R}^{(n,N-n)}\left\{f\right\}(\boldsymbol{\omega}),$$

211 where

$$\widehat{\mathcal{R}^{(n,N-n)}} \{f\}(\boldsymbol{\omega}) = \sqrt{\frac{N}{n!(N-n)!}} \frac{(-j\omega_1)^n(-j\omega_2)^{N-n}}{||\boldsymbol{\omega}||^N}} \widehat{f}(\boldsymbol{\omega}).$$
(3)

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According to Eq. (3), the product of $j\omega_1$ and/or $j\omega_2$ in the numerator followed by division with the norm of $\boldsymbol{\omega}$ produces allpass filters that only retain phase information that characterizes directions (Depeursinge et al., 2014b; Unser and Van De Ville, 2010) and the order N controls the angular selectivity of the Riesz kernels. Therefore, the Riesz kernels behave like allpass N-th order partial image derivatives. Fig. 3 illustrates the Riesz filterbanks for $N = 1, \ldots, 5$.

We also seek the steerability property of Riesz filterbanks (Freeman and Adelson, 1991; Unser and Van De Ville, 2010). In essence, this implies that a linear combination of the filterbanks may model any local rotation. When



Figure 3: Riesz filterbanks for orders up to 5 are shown here. To represent the filters on a finite spatial support, the Riesz transform was applied to an isotropic Gaussian function.



Figure 4: Steering the texture signatures Γ_c^N with an angle θ allows reducing the variability in feature values when compared to linear filtering used by e.g. CNNs. This example demonstrates that the responses of the unsteered signature (i.e., $\langle \Gamma_c^N, f_{\theta} \rangle$) on a patch rotated with θ varies strongly, which creates noise in the feature representation. However, the response of the steered signature (i.e., $\langle \Gamma_{c,\theta}^N, f_{\theta} \rangle$) is invariant to rotations of f.

looking at the maximum response over all possible orientations, steerability
allows achieving local rotation invariance at a relatively cheap computational
cost because it is not needed to re-convolve the image with rotated versions
of the kernels.

For any rotation angle $\theta \in [0, 2\pi[$, a steering matrix A_{θ} determines the corresponding response of the kernels in the filterbank to $f(\boldsymbol{x})$ for a rotation around **0** as

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$$\mathcal{R}^{N}\left\{f_{\theta}\right\}(\mathbf{0}) = \mathcal{A}_{\theta}\mathcal{R}^{N}\left\{f\right\}(\mathbf{0}), \qquad (4)$$

where f_{θ} denotes the rotation of f as $f_{\theta}(\boldsymbol{x}) = f(\mathbf{R}_{\theta}\boldsymbol{x})$ and \mathbf{R}_{θ} is a 2D rotation matrix. The use of steerability to reduce variability in feature values caused by rotations of the input patches is illustrated in Fig. 4.

²³⁴ For multi–scale analysis, the Fourier domain is partitioned using wavelets



Figure 5: A texture signature for the micronodule class is built after applying an appropriate weighing scheme for the components of a Riesz filterbank of order 5.

into several progressive dyadic bands of decreasing sizes based on Simoncelli's
isotropic multiresolution framework (Simoncelli and Freeman, 1995). The
bands control the spatial support or scale of the (allpass) Riesz kernels.

238 2.2.2. Parametric Discriminative Texture Signatures

Learned representations based on class-specific steerable texture signatures are obtained by finding a weighting scheme for the Riesz filterbanks at each scale. Fig. 5 illustrates this for a Riesz filterbank of order 5, which is used to generate a signature for micronodules. We are looking for an optimal texture signature Γ_c^N of the class c from a linear combination of the Riesz kernels as

$$\Gamma_c^N = \boldsymbol{w}^{\mathrm{T}} \boldsymbol{\mathcal{R}}^N$$

= $w_1 \boldsymbol{\mathcal{R}}^{(0,N)} + w_2 \boldsymbol{\mathcal{R}}^{(1,N-1)} + \dots + w_{N+1} \boldsymbol{\mathcal{R}}^{(N,0)},$ (5)

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where \boldsymbol{w} contains the weights of the respective Riesz kernels. A multi-scale texture signature is obtained by extending Eq. (5) using multi-scale Riesz ²⁴⁸ filterbanks (Depeursinge et al., 2012a) as

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$$\Gamma_{c}^{N} = w_{1} \left(\mathcal{R}^{(0,N)} \right)_{s_{1}} + w_{2} \left(\mathcal{R}^{(1,N-1)} \right)_{s_{1}} + \dots + w_{J(N+1)} \left(\mathcal{R}^{(N,0)} \right)_{s_{J}},$$
(6)

where s_j , for $j = 1, \ldots, J$ is the scale index.

We determine the weighing scheme using a one-versus-one SVM classi-251 fication configuration. The filter energy responses $E\left(\mathcal{R}^{(n,N-n)}\left\{f\right\}(\boldsymbol{x})\right)$ are 252 computed and regrouped for each class c versus each one from the remain-253 ing classes. SVMs then find the optimal separation in terms of minimized 254 structural risk (Guyon et al., 2002; Vapnik, 1995). Each class benefits from 255 a unique characterization with regard to each of the remaining classes. With 256 five classes, the approach is expected to lead to $5 \cdot 4 = 20$ separate optimal sig-257 natures. However, because of the optimal separation between a class A and 258 another class B is the same as that between class B and class A, the number 259 of optimal signatures reduce to 10. The optimal weights $\boldsymbol{w} = (w_1, \ldots, w_{N+1})$ 260 are directly determined from the support vectors of the optimal separa-261 tions (Depeursinge et al., 2014b). 262

263 2.2.3. Classification Using Riesz Filters

Through the approach defined previously, a class-wise texture signature Γ_c^N is obtained for each class c. Input images are then filtered using the steered texture signatures: they are steered at every position in the image to maximize their response, leading to a non-linear filtering operation. A feature space is spanned by the average energy of the steered filter responses and is complemented using a histogram of Hounsfield Units (HUs) of the patches in the spatial domain. This helps including the intensity information of the

images which is not taken into account when only wavelet domain charac-271 teristics (*i.e.*, band-pass) are utilized. The feature space is completed by 272 the number of pixels representing air in a patch as this also helps character-273 ize lung tissue (for example in the case of emphysema). In short, the feature 274 space of a patch is made up of 10 filter responses, a histogram of HUs and the 275 number of air pixels. After a series of initial investigations (not detailed in 276 this paper) into an appropriate value for the Riesz order N, a value of 5 was 277 chosen, as it was providing a good trade-off between directional specificity 278 and regularization. For N=5, 10 texture signatures of length (N+1)*J=24279 each are obtained. To create the final input feature vector, the $24 \cdot 10=240$ 280 variables obtained in the previous step are concatenated with the 22 variables 281 from the histogram and also with one last variable for air content. As a re-282 sult, a feature vector of length 263 is obtained for each patch. Once the final 283 Riesz feature vector is built, we train a Softmax classifier that maps from 284 the 263 Riesz feature vector to the 5 ILD classes. The softmax classifier uses 285 the same hyperparameters for the training of the DL feature classification 286 alone, in order to evaluate the discriminatory power of the features itself. 287 The details of the softmax classifier are discussed in section 2.4. 288

289 2.3. Tissue Characterization With Deep CNNs

DL has shown significant improvements for analyzing complex visual patterns, reaching human performance in various tasks. The CNN is the most prominent DL technique for computer vision. A CNN is a particular set of supervised multi-layer perceptron architectures. CNNs are biologically inspired by the local activations of the visual cortex (LeCun et al., 2015). Similarly to Riesz filterbanks, these local activations can be thought of like a bank of filters that act on certain areas of the input (*i.e.*, receptive fields).
Due to overlap, one may find local correlation via convolutions (Depeursinge
et al., 2017a).

Formally, given an input vector \boldsymbol{x} (which can be the output of an earlier layer), the computation of a unit \boldsymbol{a} in a layer of the neural network is a non-linear weighted sum:

$$a(\boldsymbol{x}) = \sigma(\mathbf{W}\boldsymbol{x}) = \sigma(\sum_{j=1}^{M} w_j x_j + b), \qquad (7)$$

where W is the weight matrix of the network for that layer with dimensional-303 ity M, and b is the bias term. Several activation functions $\sigma(\cdot)$ are proposed in 304 the DL literature. Rectified Linear Units (ReLUs), where $\sigma(x) = \max(0, x)$, 305 are consistently used in many applications because of their efficient gradient 306 propagation that avoids vanishing or exploding gradients and also for their 307 efficient computation as they only require a comparison. In CNNs, one is 308 interested in learning small filters q that capture the spatial correlation in 309 the input. Formally, the output of a convolution unit h_j is computed as 310

311
$$h_j(\boldsymbol{x}) = \sum_{i=1}^{C} (f_i * g_{ij})(\boldsymbol{x}),$$
 (8)

where the convolution is computed in a $P \times Q$ input window of the original image as

$$(f_i * g_{ij}) = \sum_{p=1}^{P} \sum_{q=1}^{Q} f_i(p,q) g_{ij}(x_1 - p, x_2 - q).$$
(9)

These matrix operations are efficiently vectorized to leverage the parallel capabilities of the Graphical Processing Units (GPUs). In contrast with the Riesz filter analysis, where the local rotation invariance is explicitly hardcoded in the model, DL learns relative rotation–invariance with directionally insensitive filters and multiple oriented versions of directional filters in a model with millions of free parameters (Gonzalez et al., 2016). This permits learning higher-level patterns thanks to the non-linear hierarchical composition of low-level features (Song et al., 2015) at the cost of being more prone to overfitting if the model is not regularized accordingly.

Training such large networks for medical tasks can be unfeasible due to 324 the lack of annotated data to train the model. An exciting alternative is to 325 use knowledge gained in other tasks where a large amount of data is avail-326 able. This is known as transfer learning, where a model that was initially 327 trained using a large amount of labeled data is then fine-tuned (Rozant-328 sev and Fua, 2016) to a new dataset where a fewer annotated samples are 329 available, thus leveraging the filters learned in the first dataset to serve as 330 a starting point to learn the optimal filters in the new dataset. Notably, 331 the use of pre-trained models to recognize objects in natural image settings 332 could be helpful in many medical tasks because of the following two aspects. 333 First, the layers and units in the network that recognize primitive features 334 (e.q., edges and textures) are shared across different visual contents. Second, 335 reusing a pre-trained deep network sets the state of the optimization prob-336 lem near a local optimum which is beneficial for both the performance and 337 earlier training convergence. Transfer learning has also shown to be useful 338 for faster convergence in medical scenarios where a lack of annotated data is 339 common (Janowczyk and Madabhushi, 2016). 340

For characterizing the high-level patterns in the five classes of our ILD dataset, we propose the extraction of a deep learning representation of all ILD patches from the Inception V3 deep learning architecture. This network

computes representations in a multi-scale fashion by reusing the outputs of 344 the first layers to feed later ones as well as intermediate convolution modules, 345 thus keeping the computational burden under control (Szegedy et al., 2015). 346 The principal feature of the inception architecture is the module that 347 computes $a(\mathbf{x})$ in each layer. This module uses filters g of sizes 3×3 and 348 5×5 pixels that are then arranged and concatenated with the help of 1×1 349 convolutions to shrink the number of channels of the input (or previous layer 350 output). They are then fed into the next unit by channel-wise concatenating 351 all the output filters (Szegedy et al., 2015). For augmenting the invariance 352 of the network, we augment the number of labeled samples per class by 353 producing five labels–preserving patches per sample. Three of them were 354 generated by rotating the original patch by 90, 180 and 270 degrees; the 355 other two were obtained by reflecting the patch along the x and y axes 356 respectively. 357

In the experimental setup, training all the weights from the network from 358 random initializations yields slightly worse results than fine-tuning the net-350 work with pre-trained weights on ImageNet, confirming the previous results 360 of Yosinski et al. (2014) where the authors study that transferring features 361 even from seemingly distant tasks can be better than using a random feature 362 initialization. Thus, in the following subsections when we write DL features, 363 we make a reference to fine-tuned ImageNet pre-trained weights from the in-364 ception V3 architecture. The only change necessary in our setup in order to 365 extract the features with the fine-tuned weights is to up-sample each original 366 patch to 256×256 pixels and repeating the gray-scale value matrix in three 367 different channels, to match the input size of the pre-trained architecture. 368



(a) Feature vectors are separately extracted from image patches using a Deep Learning and a Riesz-wavelet-based approach.



(b) The separate feature vectors are combined into a single vector after applying softmax classification.

Figure 6: The overall schema for the proposed late fusion approach is presented in two inter-connected parts: (a) and (b).

369 2.4. Combining Riesz Filters and Deep CNNs

Our approach to combine the Riesz and DL features is related to the one of learning a mixture of experts Masoudnia and Ebrahimpour (2014); Jacobs et al. (1991), particularly the mixture of MLP experts that learn a linear combination of the output vectors of multi-layered perceptron *experts* that specializes in a local region of the space of possible input vectors. Furthermore, we also performed experiments to assess at which fusion level the classifier better exploits the complementary information:

Early feature vector fusion: Given the two feature vectors, a simple 377 approach is to concatenate them into a single image representation and to 378 train a supervised classifier C on top of this joint representation, i.e., $x_f^i =$ 379 $[x_R^i, x_D^i]$, where $x_R^i \in \mathbb{R}^{263}$ is the Riesz feature vector and $x_D^i \in \mathbb{R}^{1024}$ is 380 an extracted embedding vector of the DL architecture as described below. 381 Formally, this corresponds to the direct sum of the Riesz and the DL feature 382 vector spaces: $X_f = X_R \oplus X_D$ thus, dim $(X_f) = \dim(X_R) + \dim(X_D)$. In 383 this fusion scheme, the interaction between the features is expected to help 384 the individual classifiers. 385

Late probability fusion: This approach consists of simply multiplying the output probability of each of the classifiers.

For a fair comparison of all five configurations (*i.e.*, Riesz, DL, early and late fusion, a softmax classifier with an intermediate hidden layer was trained using the same hyper-parameters. Softmax classifiers have proven to be useful when combining features from several sources in medical imaging (Otálora et al., 2015).

³⁹³ For the deep learning representation, a 1024–dimensional feature vector

is extracted from the layer with the largest area covered in the input image (*i.e.*, with the largest receptive field). This happens to be the layer preceding the classification layer: the *pool5* layer that carries all the different learned patterns from the previous layers.

The output of the classifier represents the probability for a patch to be classified as one of each of the 5 ILD classes. To assess that the performance gains come from the interaction of either the representations or the output probabilities, and not from the random initializations of the weight matrices that might lead to different local minima, an ensemble of three individual classifiers (trained with Riesz or DL features) are trained to have more robust predictions.

405 2.5. Softmax Classifier

To train the weights Θ of the softmax model mapping the feature vectors to class probabilities, the following cost function is minimized with a stochastic gradient descent procedure:

$$C(\Theta) = -\frac{1}{M} \left[\sum_{i=1}^{M} \sum_{j=1}^{K} \mathbb{I}\{y^{(i)} = j\} * \right]$$

$$\log \left(\frac{\exp \Theta_j x^{(i)}}{\sum_{l=1}^{K} \exp \Theta_l x^{(i)}} \right) + \frac{\rho}{2} \sum_{i=1}^{K} \sum_{j=1}^{N} \Theta_{ij}^2,$$
(10)

409

where M stands for the number of samples, N for the number of units, and K is the number of classes. ρ is the weight decay parameter that penalizes large values for parameters. The representation of an unseen test patch $X \in \mathbb{R}^{DIM}$, where DIM is the dimensionality of the feature space, which can be either 1287, 1024 or 263, for the early fusion, DL and Riesz feature vectors respectively, is then classified as class c by calculating a probability:

$$p(y^{c} = 1 | x; \Theta) = \frac{\exp(\Theta_{1}x)}{\sum_{l=1}^{K} \exp(\Theta_{l}x)}.$$
(11)

A patch belongs to the c class if $p(y^c = 1 | x; \Theta) > t$, where t is a threshold 417 deciding firm class membership. As this varies across the folds, we report the 418 average Receiver Operating Characteristic (ROC) curves and their respective 419 Area Under the Curve (AUC) for each of the five classes and each fold. The 420 number of units N in the hidden layer was explored in the set $\{32, 64, 128\}$ 421 with robust performance and we finally set it to 64 units for all experiments. 422 The other parameters of the softmax classifier were the learning rate, decay, 423 and momentum; they were set to 10^{-3} , 10^{-6} and 0.9, respectively. The 424 accelerated gradient method of Nesterov was used as a parameter in the 425 stochastic gradient descent optimizer. 426

Because the fused feature space is high-dimensional and the DL feature 427 vector is approximately four times larger than the Riesz representation, the 428 fused vector tends to reflect the performance of the DL classifier alone, leaving 429 the complementary information out. To alleviate this, we performed a late 430 fusion approach as follows. First, a single softmax classifier is trained for each 431 representation. Then, the output probability vector of the two classifiers is 432 multiplied element-wise to obtain a weighted probability vector to perform 433 the final classification. The proposed combinations are depicted in Fig. 6. 434

435 2.6. Parallel Computing

416

436 Since the calculation of steered Riesz signatures implies an iteration of
 437 all individual pixels in a patch, it is highly computationally expensive but

⁴³⁸ also highly parallelizable. On typical workstations, this step can take a pro⁴³⁹ hibitively large amount of time. Using advances made in (Vizitiu et al.,
⁴⁴⁰ 2016), we reduce the computation time by a factor of up to 30 times through
⁴⁴¹ a dedicated GPU-based implementation.

442 **3. Results**

443 3.1. Experimental Results

The Caffe DL framework (Jia et al., 2014) was used to train and extract 444 features from the Inception V3 model. RGB replication of the grayscale 445 patches and scaling from square patches of length 33 pixels to a length of 446 256 pixels was performed in order to be in line with the input layer of the 447 architecture and use the pre-trained weights. The number of epochs was set 448 to 30, but an early convergence up to the five epoch was achieved for all folds. 449 The learning rate in all cases was initially set to 0.0001 and was decreased 450 according to an exponential decay with $\sigma = 0.95$. We used the Keras² DL 451 framework with the TensorFlow back-end for all the softmax models trained, 452 using the hyperparameters previously described in subsection 2.5. 453

⁴⁵⁴ MATLAB was used for the Riesz-related calculations. First, for each ⁴⁵⁵ slice in the ILD database, square patches of length 33 pixels were extracted ⁴⁵⁶ from the annotations present. A patch is defined as any 33×33 square region ⁴⁵⁷ found to lie with at least 75% of it within the annotated region and the center ⁴⁵⁸ of which is separated by at least half a patch length from the respective ⁴⁵⁹ centers of other extracted patches. The patch size in pixels was chosen after

²https://keras.io/, as of February 2018.

investigating patch sizes that yield good results and that generate a sufficient
number of patches for training, validation, and testing. Fig. 9 illustrates the
extraction of patches. In total, 14,594 patches are found in this manner, and
a breakdown of the set in terms of classes represented is provided in Table 2.

464 3.1.1. Riesz features only

We first construct the feature vector representing each patch. The dis-465 tribution of grayscale values between -1000 HU (value for air) and 650 HU 466 (value for bone) in each patch is divided into 22 bins, which ensures a right 467 balance of granularity in spatial-domain representation and low dimension-468 ality. The number of air pixels in a patch is also noted. The energy of the 469 filter response of each patch to each of the ten weighted Riesz kernels at J=4470 scales, which ensures sufficient coverage of spatial frequencies in the Fourier-471 domain, completes the feature space. In other words, for N=5, 10 texture 472 signatures of length (N + 1) * J = 24 each are extracted. Concatenating the 473 $24 \cdot 10 = 240$ variables thus obtained with the 22 histogram bins and the air 474 content value yields the final feature vector with 263 dimensions. After all 475 the feature vectors are computed, the softmax classifier is trained, and its 476 performance on the test patches is evaluated. The recall for the Riesz fea-477 tures alone is displayed in the second row in Table 3, the model reached a 478 fold-wise average AUC of 0.924 and an average accuracy of 74.4%. 479

480 3.1.2. Deep CNN features only

The average accuracy for the four folds of the DL model was 77.1%. When using the weights of the model trained with the ImageNet dataset, the features generalized more achieving a slightly improved average accuracy



Figure 7: The aggregated confusion matrices for the four folds, of the five compared methods, is displayed. Percentages of the total number of patches are inside each cell.

of 78.6%. Once the features were extracted, we trained the softmax model
using the hyperparameters described in subsection 2.5, the model reached a
fold-wise average AUC of 0.932.

487 3.1.3. Ensemble of three CNN models

An ensemble model consisting of the fusion of three weight initialization 488 of the InceptionV3 architecture was trained to have a better estimate of the 489 performance of the CNN features, not relying only on the optima found in 490 one single CNN model training. This model takes as input the concatenated 491 vectors $x \in \mathbb{R}^{3072}$ of the three trained CNN's representation. The same soft-492 max gating model architecture of the single DL model is trained with the 493 fused vectors. The average accuracy was 77.9%, and the fold-wise average 494 AUC in the ensemble model was 0.937. The confusion matrix as displayed in 495 Figure 7 shows a better performance for the healthy, ground glass, and mi-496 cronodules classes while slightly worsening the results of the single DL model 497 in the fibrosis and emphysema classes. This result suggests that the results 498 of the single model are relatively robust to the weight initialization of the 490 network, and it stands to reason to not use more than one DL feature vector 500 in the fusion with the Riesz features since the dimension of the combination 501 will increase unnecessarily. 502

⁵⁰³ 3.1.4. Combining Riesz and Deep CNN Representations

The early fusion approach of the concatenation of both DL and Riesz feature vectors yielded 78.1% average fold accuracy. An AUC performance of 0.931 was also noted, which is almost identical to the performance of the DL features alone. Because the fused feature space is high-dimensional and the DL feature vector is approximately four times larger than the Riesz representation, the fused vector tends to reflect the performance of the DL classifier alone, dismissing the complementary of the two representations. To alleviate this, we implemented a late fusion, which obtained the best AUC performance of 0.948 as depicted in Fig. 8 and this shows that it makes the best use of both classifiers.

514 3.1.5. Combining Riesz and Deep CNN Representations

515 3.2. Statistical Significance of the Performance Comparisons

To assess the statistical significance of the difference between the results of the classifiers for all the classes together, we computed the McNemar test (Dietterich, 1998). For the test, the null hypothesis is not having a significant difference between the classifier results, and the alternative hypothesis being the opposite, *i.e.*, the mean of their results are distinct enough and cannot be due to a random process.

We concatenated the class predictions for each classifier in each fold and computed the number of times that a specific classifier A has guessed the correct class and a certain classifier B did not. Then, we computed the same number after inverting the classifier predictions, and these two sums were passed as parameters to the mid-p-test. If the p-value is less than 0.05, the results are considered to be statistically significant (Fagerland et al., 2013). The results of the test are presented in Table 1.

529 4. Discussions

The results obtained using our method are compared with the results obtained by other authors who used the same ILD dataset but with possible





(b) ROC curves for fibrosis and micronodules.

Figure 8: ROC curves of the average performance in the four folds for each class using the late fusion approach depicted here. Healthy, Emphysema and Ground Glass classes, having a better AUC than the other approaches, benefit the most from the fusion.

Table 1: p-values for the comparison of our four approaches

Comparison	<i>p</i> -value
DL vs Riesz	7.949e-14
(DL Riesz) early fusion vs (DL Riesz) late fusion	2.232e-85



Figure 9: Overlapping patches of size 33–by–33 pixels are extracted from an annotated slice.

Table 2: The classwise distribution of patches extracted from the ILD database is shown here.

Class	Number of patches	
Healthy	3011	
Emphysema	407	
Ground Glass	2226	
Fibrosis	2962	
Micronodules	5988	
Total	14594	

			Class		
Method	Н	Е	G	F	М
Riesz (biased)	0.726	0.573	0.727	0.824	0.875
Riesz	0.756	0.334	0.707	0.818	0.726
DL only	0.478	0.546	0.729	0.847	0.855
Early Fusion	0.479	0.516	0.723	0.855	0.858
Late Fusion	0.634	0.543	0.767	0.881	0.875
(Song et al., 2013)	0.876	0.806	0.827	0.812	0.811
(Shin et al., 2016)	0.680	0.910	0.700	0.830	0.790
(Depeursinge et al., 2012b)	0.673	0.787	0.714	0.827	0.816
(Depeursinge et al., 2012a)	0.827	0.727	0.684	0.842	0.835
(Foncubierta-Rodríguez et al., 2012)	0.053	0.745	0.496	0.746	0.519
(Depeursinge et al., 2011a)	0.775	0.733	0.723	0.845	0.805
(Li et al., 2013)	0.760	0.670	0.700	0.740	0.840
(Depeursinge et al., 2011b)	0.790	0.692	0.593	0.805	0.702
(Gao et al., 2016)	0.914	0.827	0.815	0.891	0.880
(Song et al., 2015)	0.885	0.796	0.800	0.854	0.872

Table 3: Recalls obtained for our methods versus others in the literature are shown here.

variations in terms of the evaluation methodology. Although the dataset
used is the same, the exact validation scheme differs from one method to
another according to the selection of patches (percentage lying within the
ROI), patch size, distribution of the classes, and cross-validation schemes.
Notwithstanding, Table 3 details the accuracies for the different tissue types
obtained by our method and reported by others but they need to be read
with care due to the differences in exact evaluation.

A first observation is that when the dataset is carefully divided up in 539 order to ensure that the same patient does not contribute patches to both 540 the training and test sets, the performance of the same Riesz-based SVM 541 classification method drops significantly on the whole (first versus second 542 rows of Table 3). This proves beyond doubt that bias is present when the 543 above separation step is not explicitly taken. Since many of the existing 544 methods present no evidence of explicitly applying such a step; their reported 545 performance values are at risk of being erroneously higher than they should 546 be. 547

Table 3 shows that there is some room for improvement in the classifica-548 tion of the emphysema class. Indeed, only 407 patches with identified em-549 physema are encountered in the ILD database while the next least frequent 550 disease class is ground glass with 2226 patches. This is a notable disparity, 551 and we would argue that our learning approaches for emphysema are less 552 well trained as compared to the other classes due to a much lower number 553 of patches used for training. Besides, emphysema has very large intra-class 554 variations and would require learning several steerable models or signatures 555 per class. We contend that the use of more patches belonging to that class for 556 training and the use of more than one signature for emphysema in subsequent 557 work would significantly improve the overall classification accuracy. 558

Finally, the classification accuracy of four different approaches are compared: deep CNN features alone, Riesz features alone, early fusion of the feature vectors and late fusion of the class probability for each classifier. Moreover, an ensemble of three deep CNN architectures was found to only add a negligible improvement to the results of a single network. An approach

that uses multiple architectures at training time, or using the dropout tech-564 nique Srivastava et al. (2014) in some of the layers could lead to more sig-565 nificant improvements. The comparison was made on the same basis using a 566 softmax layer with the same hyperparameters. Furthermore, we assessed the 567 statistical significance of the results of the classifiers by applying the McNe-568 mar test. The observed p-values are much lower than 0.05, demonstrating 569 important statistical significance of the presented differences. Nevertheless, 570 there is a more significant gap, thus a smaller p-value, between the early and 571 late fusion classifiers. This could be because when the early fusion of the fea-572 ture vectors is performed, the representations are merged in the intermediate 573 layer of the softmax classifier, leading to more aligned representations than 574 in the case of the late fusion, where we multiply both independent proba-575 bilities. On the other hand, for the separate feature classifiers, some of the 576 learned features in the early layers of DL classifier likely resemble the filter-577 banks learned using Riesz aligned texture signatures. This would explain the 578 similar predictions in that particular case. 570

580 5. Conclusions

In this paper, we show that late-fusing learned tissue representations based on Riesz and Deep CNN's for texture characterization yields performance gains over each approach separately or even early fusion. We showed that this is because is not dependent on the feature vector dimensionality but only on the independent probability of the classifiers. We believe that further performance gains can be achieved by investigating new methods of fusing Riesz-based and DL-based features, taking advantage of the complementarity of both sources of visual content from the ILD patches (Depeursinge andMüller, 2010).

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